p-adic numbers are an essential part of modern number theory. In this talk, we will introduce p-adic numbers through two analogies: a spiritual motivation for p-adic numbers using an analogy with rational functions and a concrete construction of p-adic numbers by analogy with the real numbers. We will then discuss some of the properties that make p-adic numbers seem strange and interesting!